

Concolic Testing of Functional Logic Programs

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Program Testing

Check correctness of programs via testing

⇒ But writing test cases manually is time consuming and tedious...

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(Automated) Testing Tools and Libraries:

- Random testing
- Property-based testing
- Symbolic Execution
- Concolic Execution

Concolic Execution

Goal: Find enough test cases for full program coverage

Basic Idea: **Concrete Execution** drives **Symbolic Execution**

- Execute program with concrete input data
- Collect symbolic information during concrete execution
- Information corresponds to constraints along *one* execution path
- Negate and solve constraints systematically to search for *alternative* execution paths

Concolic Execution Example

```
nthElem [] _ = Nothing
nthElem (x : xs) n | n == 0 = Just x
                   | n > 0 = nthElem xs (n - 1)
```

Example (Initial Call: `nthElem [False] 0`)

Concrete Execution:

- selects second program rule
- yields the result `Just False`

Symbolic Execution:

- starts with symbolic function call `nthElem yss ns`
- constrains them whenever a branch decision is made

Path Constraints:

- $ys_s = xs : xs_s \wedge n_s = 0$
- Compute input data for alternative execution paths (`nthElem [] 0`)

Curry - A Functional Logic Programming Language

- Haskell-like syntax
- Higher order functions, non-strict semantics, lazy evaluation
- Non-determinism, free variables

Curry

```
not True  = False
not False = True

map _ []      = []
map f (x : xs) = f x : map f xs

insertND x []      = [x]
insertND x (y : ys) = x : y : ys
insertND x (y : ys) = y : insertND x ys
```

Example Calls

```
> map not [True, False]
[False, True]

> insertND 42 [1, 2]
[42, 1, 2]
[1, 42, 2]
[1, 2, 42]

> not x where x free
{x = False} True
{x = True} False
```

Concolic Execution Scheme of Curry

Curry Concolic Testing Interpreter (*ccti*)

Input Program P with initial call of the function to be tested e

Output Set of test cases, i.e. input data and corresponding results

Translation of Curry to FlatCurry

Curry

```
nthElem [] _ = Nothing
nthElem (x : xs) n | n == 0 = Just x
                   | n > 0 = nthElem xs (n - 1)
```

```
insertND x [] = [x]
insertND x (y : ys) = x : y : ys
insertND x (y : ys) = y : insertND x ys
```

FlatCurry

```
nthElem xs n = case xs of
  [] -> Nothing
  y:ys -> case n == 0 of
    True -> Just y
    False -> case n > 0 of True -> nthElem ys (n-1)
                        False -> failed
```

```
insertND x xs = case xs of
  [] -> [x]
  y:ys -> (x : y : ys) ? (y : insertND x ys)
```


Translation of Curry to FlatCurry

Curry

```
nthElem [] _ = Nothing
nthElem (x : xs) n | n == 0 = Just x
                  | n > 0 = nthElem xs (n - 1)
```

```
insertND x [] = [x]
insertND x (y : ys) = x : y : ys
insertND x (y : ys) = y : insertND x ys
```

FlatCurry

```
nthElem xs n = case1 xs of
  [] -> Nothing
  y:ys -> case2 n == 0 of
    True -> Just y
    False -> case3 n > 0 of True -> nthElem ys (n-1)
                          False -> failed
```

```
insertND x xs = case4 xs of
  [] -> [x]
  y:ys -> (x : y : ys) ? (y : insertND x ys)
```

Trace Symbolic Information in Deterministic Programs

```
nthElem xs n = case1 xs of
  []    -> Nothing
  y:ys  -> case2 n == 0 of
    True  -> Just y
    False -> case3 n > 0 of True  -> nthElem ys (n-1)
                          False -> failed
```

Concrete Execution

```
nthElem [False] 0
```

Symbolic Trace

Trace Symbolic Information in Deterministic Programs

```
nthElem xs n = case1 xs of
  []    -> Nothing
  y:ys  -> case2 n == 0 of
    True  -> Just y
    False -> case3 n > 0 of True  -> nthElem ys (n-1)
                          False -> failed
```

Concrete Execution

```
nthElem [False] 0
```

Symbolic Trace

```
[]
```

Trace Symbolic Information in Deterministic Programs

```
nthElem xs n = case1 xs of
  []    -> Nothing
  y:ys  -> case2 n == 0 of
    True  -> Just y
    False -> case3 n > 0 of True  -> nthElem ys (n-1)
                          False -> failed
```

Concrete Execution

```
nthElem [False] 0
=>* case1 [False] of ...
```

Symbolic Trace

```
[]
[]
```

Trace Symbolic Information in Deterministic Programs

```
nthElem xs n = case1 xs of
  []    -> Nothing
  y:ys  -> case2 n == 0 of
    True  -> Just y
    False -> case3 n > 0 of True  -> nthElem ys (n-1)
                          False -> failed
```

Concrete Execution

```
nthElem [False] 0
=>* case1 [False] of ...
=>* case2 0 == 0 of ...
```

Symbolic Trace

```
[]
[]
[(case1, 2/2, xsS, (:))]
```

Trace Symbolic Information in Deterministic Programs

```
nthElem xs n = case1 xs of
  []    -> Nothing
  y:ys  -> case2 n == 0 of
    True  -> Just y
    False -> case3 n > 0 of True  -> nthElem ys (n-1)
                          False -> failed
```

Concrete Execution

```
nthElem [False] 0
=>* case1 [False] of ...
=>* case2 0 == 0 of ...
=>* Just False
```

Symbolic Trace

```
[]
[]
[(case1, 2/2, xss, (:))]
[(case1, 2/2, xss, (:)), (case2, 1/2, ns == 0)]
```

Trace Symbolic Information in Deterministic Programs

```
nthElem xs n = case1 xs of
  []    -> Nothing
  y:ys  -> case2 n == 0 of
    True  -> Just y
    False -> case3 n > 0 of True  -> nthElem ys (n-1)
                          False -> failed
```

Concrete Execution

```
nthElem [False] 0
=>* case1 [False] of ...
=>* case2 0 == 0 of ...
=>* Just False
```

Symbolic Trace

```
[]
[]
[[case1, 2/2, xss, (:)]
[[case1, 2/2, xss, (:), (case2, 1/2, ns == 0)]
```

- Program branches: case expressions and non-det. choices
- Trace symbolic information: case ids, branch numbers, symbolic variables, matching constructors
- Comparison operations on numerical literals: associated constraint

Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]  
                        y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
```


Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]  
                        y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
```

```
[]
```

Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]
                    y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
⇒* case4 [False] of ...
```

```
[]
[]
```

Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]
                    y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
⇒* case4 [False] of ...
⇒* (True : False : []) ? (False : insertND True [])
```

```
[]
[]
[(case4, 2/2, xss, (:))]
```

Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]
                  y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
⇒* case4 [False] of ...
⇒* (True : False : []) ? (False : insertND True [])
```

```
[]
[]
[(case4, 2/2, xss, (:))] ? [(case4, 2/2, xss, (:))]
```

Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]
                  y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
=>* case4 [False] of ...
=>* (True : False : []) ? (False : insertND True [])
=>* {[True, False]}
```

```
[]
[]
[(case4, 2/2, xsS, (:))] ? [(case4, 2/2, xsS, (:))]
{[(case4, 2/2, xsS, (:))]}
```

Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]
                  y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
⇒* case4 [False] of ...
⇒* (True : False : []) ? (False : insertND True [])
⇒* {[True, False]} ∪ (False : case4 [] of ...)
```

```
[]
[]
[(case4, 2/2, xss, (:))] ? [(case4, 2/2, xss, (:))]
{[(case4, 2/2, xss, (:))]} ∪ [(case4, 2/2, xss, (:))]
```

Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]
                  y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
⇒* case4 [False] of ...
⇒* (True : False : []) ? (False : insertND True [])
⇒* {[True, False]} ∪ (False : case4 [] of ...)
⇒* {[True, False]} ∪ {[False, True]}
```

```
[]
[]
[(case4, 2/2, xss, (:))] ? [(case4, 2/2, xss, (:))]
{[(case4, 2/2, xss, (:))]} ∪ [(case4, 2/2, xss, (:))]
{[(case4, 2/2, xss, (:))]} ∪ [(case4, 2/2, xss, (:)), (case4, 1/2, yss, [])]
```

Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]
                  y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
⇒* case4 [False] of ...
⇒* (True : False : []) ? (False : insertND True [])
⇒* {[True, False]} ∪ (False : case4 [] of ...)
⇒* {[True, False]} ∪ {[False, True]}
⇒* {[True, False], [False, True]}
```

```
[]
[]
[(case4, 2/2, xss, (:))] ? [(case4, 2/2, xss, (:))]
{[(case4, 2/2, xss, (:))]} ∪ [(case4, 2/2, xss, (:))]
{[(case4, 2/2, xss, (:))]} ∪ [(case4, 2/2, xss, (:)), (case4, 1/2, yss, [])]
{[(case4, 2/2, xss, (:))], [(case4, 2/2, xss, (:)), (case4, 1/2, yss, [])]}
```


Trace Symbolic Information in Non-Deterministic Programs

```
insertND x xs = case4 xs of []    -> [x]
                  y:ys -> (x : y : ys) ? (y : insertND x ys)
```

```
insertND True [False]
⇒* case4 [False] of ...
⇒* (True : False : []) ? (False : insertND True [])
⇒* {[True, False]} ∪ (False : case4 [] of ...)
⇒* {[True, False]} ∪ {[False, True]}
⇒* {[True, False], [False, True]}
```

```
[]
[]
[(case4, 2/2, xss, (:))] ? [(case4, 2/2, xss, (:))]
{[(case4, 2/2, xss, (:))]} ∪ [(case4, 2/2, xss, (:))]
{[(case4, 2/2, xss, (:))]} ∪ [(case4, 2/2, xss, (:)), (case4, 1/2, yss, [])]
{[(case4, 2/2, xss, (:))], [(case4, 2/2, xss, (:)), (case4, 1/2, yss, [])]}
```

- Encapsulate non-determinism ⇒ multisets of results and traces

Semantics for Concolic Execution

- Evaluate an expression e w.r.t. a heap Γ and an incoming symbolic trace T to a value v , an updated heap Δ and an extended trace Υ

$$\Gamma, T : e \Downarrow \Delta, \Upsilon : v$$

- Heap: Map variables to expressions or mark them as **free**

$$\Gamma, \Delta, \Theta \in \mathit{Heap} = \mathcal{V} \rightarrow \{\mathit{free}\} \uplus \mathit{Exp}$$

- Symbolic Trace: List of symbolic information for selected branches

$$T, \Upsilon, X \in \mathit{Trace}$$

Semantics for Concolic Execution (Excerpt)

Extension of FlatCurry semantics [Hanus, Peemöller - WFLP 2014]

Value $\Gamma \vdash v \Downarrow \Gamma \vdash v$ where $v = c(\overline{x}_n)$ or $v \in \mathcal{V}$ with $\Gamma[v] = \text{free}$

VarExp
$$\frac{\Gamma \vdash e \Downarrow \Delta \vdash v}{\Gamma[x \mapsto e] \vdash x \Downarrow \Delta[x \mapsto v] \vdash v}$$
 where $e \notin \{\text{free}\}$

Or
$$\frac{\Gamma \vdash e_i \Downarrow \Delta \vdash v}{\Gamma \vdash e_1 ? e_2 \Downarrow \Delta \vdash v}$$
 where $i \in \{1, 2\}$

Select
$$\frac{\Gamma \vdash x \Downarrow \Delta \vdash c(\overline{y}_n) \quad \Delta \vdash \sigma(e_i) \Downarrow \Theta \vdash v}{\Gamma \vdash \text{case}_{id} x \text{ of } \{ \overline{p_k \rightarrow e_k} \} \Downarrow \Theta \vdash v}$$

where $p_i = c(\overline{x}_n), \sigma = \{ \overline{x_n \mapsto y_n} \}$

Semantics for Concolic Execution (Excerpt)

Extension of FlatCurry semantics [Hanus, Peemöller - WFLP 2014]

Value $\Gamma, T : v \Downarrow \Gamma, T : v$ where $v = c(\overline{x}_n)$ or $v \in \mathcal{V}$ with $\Gamma[v] = \text{free}$

VarExp
$$\frac{\Gamma, T : e \Downarrow \Delta, \Upsilon : v}{\Gamma[x \mapsto e], T : x \Downarrow \Delta[x \mapsto v], \Upsilon : v}$$
 where $e \notin \{\text{free}\}$

Or
$$\frac{\Gamma, T : e_i \Downarrow \Delta, \Upsilon : v}{\Gamma, T : e_1 ? e_2 \Downarrow \Delta, \Upsilon : v}$$
 where $i \in \{1, 2\}$

Select
$$\frac{\Gamma, T : x \Downarrow \Delta, \Upsilon : c(\overline{y}_n) \quad \Delta, \Phi : \sigma(e_i) \Downarrow \Theta, X : v}{\Gamma, T : \text{case}_{id} x \text{ of } \{ \overline{p}_k \mapsto e_k \} \Downarrow \Theta, X : v}$$

where $p_i = c(\overline{x}_n)$, $\sigma = \{\overline{x}_n \mapsto \overline{y}_n\}$, x_s fresh symbolic variable,
 $\Phi = \Upsilon ++ [(id, i/k, x_s, c)]$

Search Strategy of *ccti*

- Symbolic traces → paths through symbolic execution tree
- Single trace entry → node of symbolic execution tree

Search Algorithm

- 1 Update symbolic execution tree with traces / mark branches as visited
- 2 Select node closest to the root with unvisited branches
- 3 Negate path constraint of that node
- 4 Try to solve constraints along path from root to selected node
 - ▶ **sat**: Compute new input data from model
 - ▶ **unsat**: Mark branches as visited and continue with 2

Selection and Solving of Path Constraints

Symbolic Trace for nthElem [False] 0

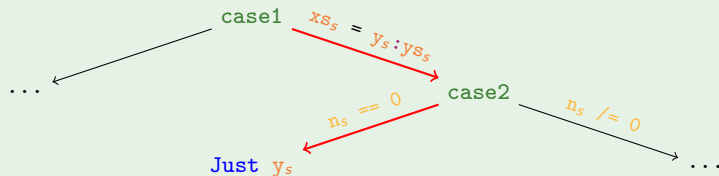
```
[(case1, 2/2, xs_s, ()), (case2, 1/2, n_s == 0)]
```

Selection and Solving of Path Constraints

Symbolic Trace for `nthElem [False] 0`

`[(case1, 2/2, xss, ()), (case2, 1/2, ns == 0)]`

Example (Symbolic Execution Tree for `nthElem`)

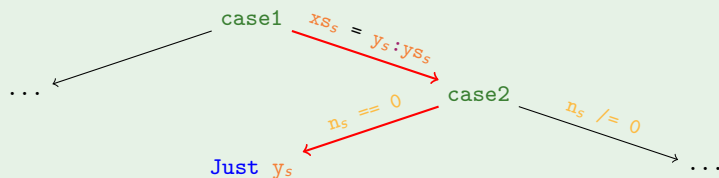


Selection and Solving of Path Constraints

Symbolic Trace for nthElem [False] 0

```
[(case1, 2/2, xss, ()), (case2, 1/2, ns == 0)]
```

Example (Symbolic Execution Tree for nthElem)



- Path constraint: $x_{s_s} = y_s : y_{s_s} \wedge n_s = 0$
- Search Strategy: Select node **case1** for negation
- Apply SMT solver to modified constraints: $\forall y_s, y_{s_s} : \neg(x_{s_s} = y_s : y_{s_s})$
- Receive input data for alternative execution path: nthElem [] 0

Application of *ccti*

Test cases found for `nthElem`

```
nthElem [False]    0 ==- Just False
nthElem []         0 ==- Nothing
nthElem [False]   1 ==- Nothing
failing $ nthElem [False] (-1)
```

Tested Function	Initial Arguments	Cases	<i>ccti</i> Tests	Minimum Tests ¹	Full Coverage
<code>nthElem</code>	<code>[False], 0</code>	3	4	3	yes
<code>insertND</code>	<code>True, []</code>	1	2	2	yes
<code>addNat</code>	<code>IHi, IHi</code>	4	9	6	yes
<code>perm</code>	<code>[False]</code>	2	1	1	no
<code>semRE</code>	<code>Lit A</code>	2	3	1	no

¹Number of test cases sufficient for full program coverage

Current Limitations of *ccti*

Curry

```
insertND x xs = case4 xs of []    -> [x]
                  y:ys -> (x : y : ys) ? (y : insertND x ys)

perm xs = case5 xs of []    -> []
                  y:ys -> insertND y (perm ys)
```

- For perm [False] *ccti* finds only single test case
- No coverage of second branch of case4
- **Problem:** Second branch of case5 is already covered by top-level call
⇒ Not considered for recursive call of perm
⇒ insertND is never called with non-empty list
- **Solution:** Apply alternative coverage criterion for search

Conclusion

- *ccti* - concolic testing of functional logic programs
- Extension of FlatCurry semantics to trace symbolic information
- Application of SMT solver for solving of path constraints
- First evaluation: applicable for test case generation
- Global branch coverage insufficient for some examples

Future Work

- Implementation of alternative strategies and code coverage criteria
- Further evaluation of *ccti*:
 - More complex programs
 - Comparison with narrowing-based test case generation (CurryCheck)